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$$a) \lim_{x \rightarrow 0} \frac{4x}{x^2 - 2x} = \left(\frac{0}{0} \right) = \lim_{x \rightarrow 0} \frac{4x}{(x)(x-2)} = \lim_{x \rightarrow 0} \frac{4}{(x-2)} = \frac{4}{-2} = -2$$

$$c) \lim_{x \rightarrow 1} \frac{x^2 - 1}{x - 1} = \left(\frac{0}{0} \right) = \lim_{x \rightarrow 1} \frac{(x-1)(x+1)}{(x-1)} = \lim_{x \rightarrow 1} (x+1) = 2$$

$$e) \lim_{x \rightarrow -2} \frac{x+2}{x^2 - 4} = \left(\frac{0}{0} \right) = \lim_{x \rightarrow -2} \frac{x+2}{(x-2)(x+2)} = \lim_{x \rightarrow -2} \frac{1}{(x-2)} = \frac{1}{-4} = -\frac{1}{4}$$

$$g) \lim_{x \rightarrow -3} \frac{x+3}{x^2 + 4x + 3} = \left(\frac{0}{0} \right) = \lim_{x \rightarrow -3} \frac{x+3}{(x+3)(x+1)} = \lim_{x \rightarrow -3} \frac{1}{(x+1)} = \frac{1}{-2} = -\frac{1}{2}$$

$$\begin{array}{r|rrr} & 1 & 4 & 3 \\ -3 & & -3 & -3 \\ \hline & 1 & 1 & 0 \end{array} \rightarrow x^2 + 4x + 3 = (x+3)(x+1)$$

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15)

$$a) \lim_{x \rightarrow 3} \frac{x^2 - x - 6}{x^2 - 3x} = \left(\frac{0}{0} \right) = \lim_{x \rightarrow 3} \frac{(x+2)(x-3)}{(x)(x-3)} = \lim_{x \rightarrow 3} \frac{x+2}{x} = \frac{5}{3}$$

$$\begin{array}{r|rrr} & 1 & -1 & -6 \\ 3 & & 3 & 6 \\ \hline & 1 & 2 & 0 \end{array}$$

$$b) \lim_{x \rightarrow 1} \frac{x^2 - 3x + 2}{x^2 - 2x + 1} = \left(\frac{0}{0} \right) = \lim_{x \rightarrow 1} \frac{(x-1)(x-2)}{(x-1)(x-1)} = \lim_{x \rightarrow 1} \frac{(x-2)}{x-1} = \frac{-1}{0} = \infty$$

$$\begin{array}{r|rrr} & 1 & -3 & 2 \\ 1 & & 1 & -2 \\ \hline & 1 & -2 & 0 \end{array} \quad \begin{array}{r|rrr} & 1 & -2 & 1 \\ 1 & & 1 & -1 \\ \hline & 1 & -1 & 0 \end{array}$$

calculemos el signo del ∞

$$\lim_{x \rightarrow 1^-} \frac{x-2}{x-1} = [x=0'9]_{-}^{-} \infty = +\infty$$

$$\lim_{x \rightarrow 1^+} \frac{x-2}{x-1} = [x=1'1]_{+}^{-} \infty = -\infty$$

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